

Design of Beams

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Questions related to specific materials, methods, and services will be addressed at the conclusion of this presentation.

Course Description

This session will review the design of masonry beams and lintels, including an examination of whether arching action can be used to reduce the loads on these elements. Deflection calculations will be reviewed, along with detailing requirements to meet code minimum and maximum reinforcement percentages. Deep beam requirements will also be covered.

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Learning Objectives

- Introduce the design masonry beams and lintels for bending moment and shear
- Describe deflection calculations for beams and lintels
- Review maximum and minimum reinforcing provisions
- Examine arching and discuss when it can be used

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Determination of Loads, Shears, and Moments

- Arching
- Beam Depth
- Beam Span

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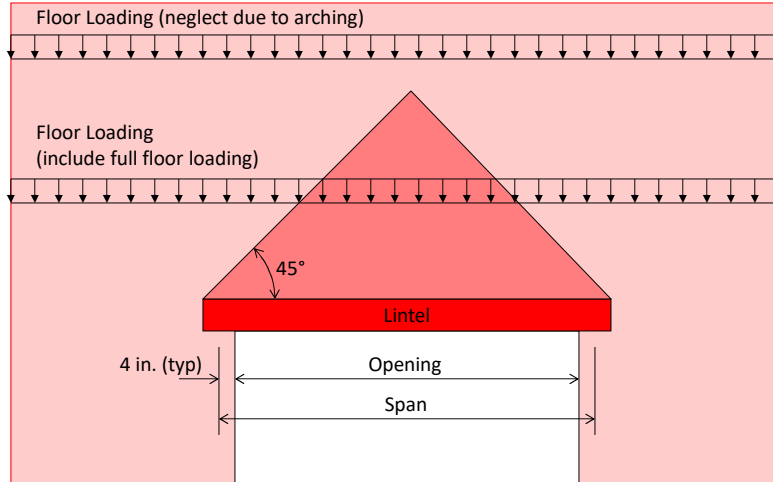
Arching



(State College, PA)

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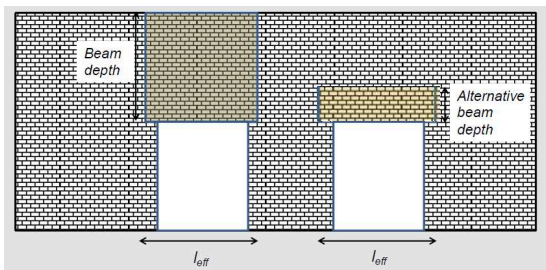
Arching



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Beam Depth

Strength Design Guide 3.3.1



TMS 402 Figure CC-5.2-2



Strength Design Guide Figure 6.3.1-3

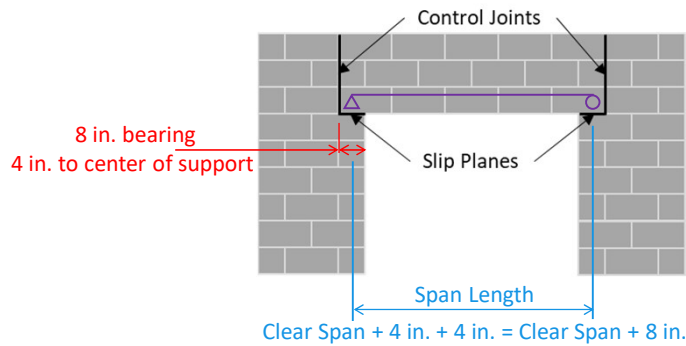
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Beam Span: Beams not built integrally with supports

Strength Design Guide 6.3.1; TMS 402 5.2.1.1.1

Span is minimum of:

- Clear span + depth of beam
- Distance between centers of supports



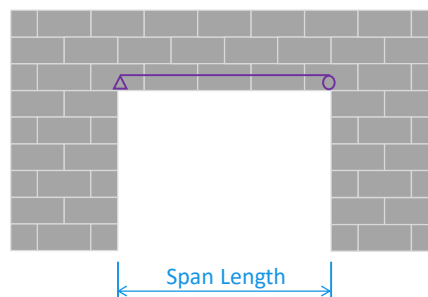
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Beam Span: Beams built integrally with supports

Strength Design Guide 6.3.1; TMS 402 is silent

Reasonable approximation: Clear span

- without significant negative moment reinforcement
- Lee et al (1983) showed end restraint reduced deflection from 20-45% of simply support



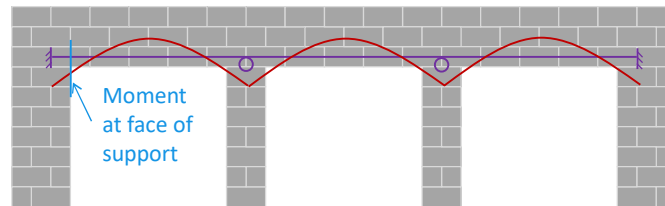
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Beam Span: Continuous

Strength Design Guide 6.3.1; TMS 402 5.2.1.1.2

Requires negative moment reinforcement (otherwise built integrally with supports)

- Span length distance between centers of support for determining moments
- Reasonable approximation: Design for moment at face of supports



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Beam Requirements

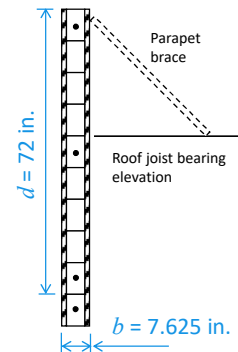
- Chapter 5
- Chapter 9

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General Beam Design

Strength Design Guide 6.3.1; TMS 402 5.2.1

- Lateral support (TMS 402 5.2.1.2)
 - Minimum of:
 - $32b$
 - $120b^2/d$
- Bearing length (TMS 402 5.2.1.3)
 - Minimum of 4 in. in direction of span



$$32b = 32(7.625 \text{ in.}) = 244 \text{ in.}$$

$$120b^2/d = 120(7.625 \text{ in.})^2/72 \text{ in.} = 96.9 \text{ in.}$$

Brace at every roof joist, which is 5 ft spacing

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Beams

Strength Design Guide 6.3.1; TMS 402 9.3.4.2

- $P_u \leq 0.05A_n f'_m$ (TMS 402 9.3.4.2.1)
- ~~The variation in longitudinal reinforcing bars in a beam shall not be greater than one bar size. Not more than two bar sizes shall be used in a beam.~~ (TMS 402 9.3.4.2.1.1)
- Beams are required to be fully grouted (TMS 402 9.3.4.2.4)

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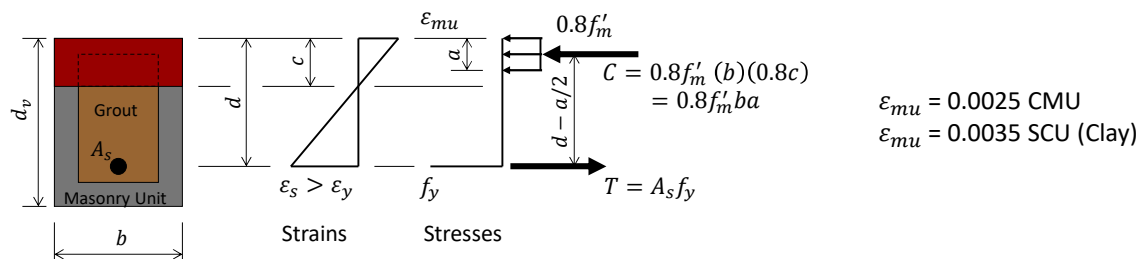
Flexural Design

- Design Moment Strength
- Flexural Design
- Minimum/Maximum Reinforcement
- Beam Construction

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Nominal Moment Capacity

Strength Design Guide 6.2.1; TMS 402 9.3.2 (Design Assumptions)



$$a = \frac{A_s f_y}{0.8 f'_m b}$$

$$M_n = A_s f_y \left(d - \frac{1}{2} \frac{A_s f_y}{0.8 f'_m b} \right)$$

$\phi = 0.9$ for flexure
(TMS 402 9.1.4.4)

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Flexural Design

Strength Design Guide 6.2.1.1

1. Determine material properties (f_y, f'_m)
2. Choose beam dimensions
 - A. Thickness: 8 in., 12 in.
 - B. Depth: if possible, choose so no shear reinforcement is required
3. Determine a , depth of compressive stress block

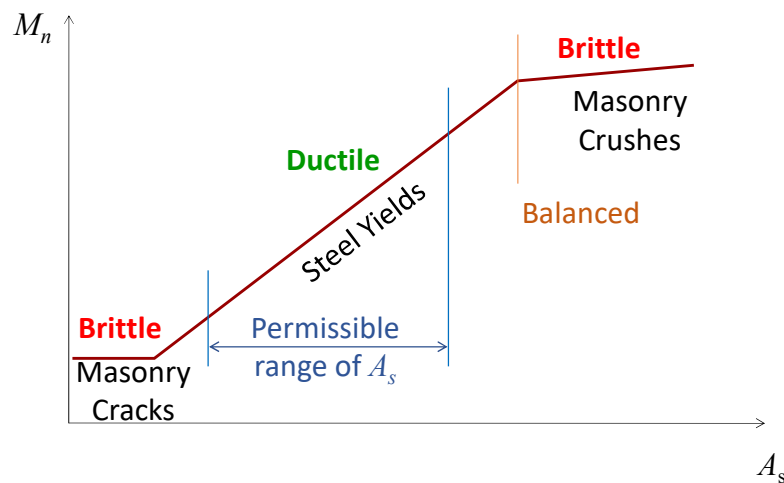
$$a = d - \sqrt{d^2 - \frac{2M_n}{0.8f'_m b}} = d - \sqrt{d^2 - \frac{2M_u}{0.8\phi f'_m b}}$$

4. Solve for $A_{s,reqd}$

$$A_{s,reqd} = \frac{0.8f'_m b a}{f_y}$$

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Reinforcement Limitations



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Minimum Reinforcement

Strength Design Guide 6.3.1.3; TMS 402 Section 9.3.4.2.2.2, 9.3.4.2.2.3

- $M_n \geq 1.3M_{cr}$, or $M_u \geq 1.17M_{cr}$
- $M_{cr} = f_r \frac{bh^2}{6} = f_r \frac{bd_v^2}{6}$
- or $A_s \geq (4/3)A_{s,reqd}$

M_{cr} = cracking moment
 f_r = modulus of rupture
 b = thickness
 $h = d_v$ = depth of beam

Flexural Tension Stress Parallel to Bed Joint	Mortar Type			
	PCL or mortar cement		Masonry Cement	
	M or S	N	M or S	N
Running bond; fully grouted	267	200	160	100
Not laid in running bond; continuous grout section parallel to bed joints	335	335	335	335

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Maximum Reinforcement

Strength Design Guide 6.3.1.2; TMS 402 Section 9.3.3.2

$$\rho_{max} = \frac{0.8(0.8)f'_m}{f_y} \left(\frac{\varepsilon_{mu}}{\varepsilon_{mu} + 1.5\varepsilon_y} \right)$$

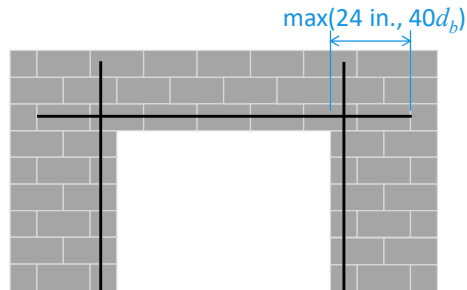
Steel Ratio	Grade 60 steel	
	Clay	CMU
ρ_{max} (f'_m in ksi)	$0.00565f'_m$	$0.00476f'_m$
$f_y = 60$ ksi	$f'_m = 3$ ksi 0.01697	$f'_m = 2$ ksi 0.00952

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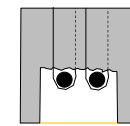
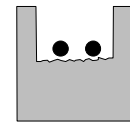
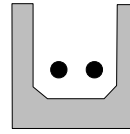
Beam Construction

Strength Design Guide 6.3.1.5

- d = depth to centroid of tension reinforcement
- For one layer of reinforcement, $d \sim (d_v - 4in.)$



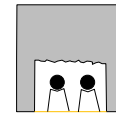
Seismic Requirements (TMS 402 7.3.2.3.1)



Wire to web



Figure courtesy of Wirebond



Support
on chairs



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Deflections

- Effective Moment of Inertia
- Deflection Requirements

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Effective Moment of Inertia

Strength Design Guide 6.3.1.1; TMS 402 Section 5.2.1.4

$$I_{eff} = I_n \left(\frac{M_{cr}}{M_a} \right)^3 + I_{cr} \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right]$$

$$I_{cr} = \frac{bk^3d^3}{3} + nA_s(d - kd)^2$$

$$k = \sqrt{(n\rho)^2 + 2n\rho} - n\rho$$

$$\rho = \frac{A_s}{bd} \quad n = \frac{E_s}{E_m}$$

I_n = net moment of inertia

I_{cr} = cracked moment of inertia

M_{cr} = cracking moment

M_a = Moment under allowable stress level loads

n = modular ratio, E_s/E_m

k = depth to neutral axis under allowable stress assumptions

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Deflection Requirements

Strength Design Guide 6.3.1.1; TMS 402 Section 5.2.1.4

- Deflection of beam or lintels supporting unreinforced masonry is limited to $L/600$, where L is span length (TMS 402 5.2.1.4.1)
- Deflections of approximately $L/300$ needed to be visible.
- Deflections do not need to be checked when $L \leq 8d$ (TMS 402 5.2.1.4.3).

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Shear

- Shear strength
- Stirrups
- Chapter 8: shear at $d/2$

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Shear Strength

Strength Design Guide 6.2.4.1; TMS 402 Section 9.3.4.1.2

Assume $M_u/(V_u d_v) = 1.0$

$$V_n = V_{nm} + V_{ns}$$

$$V_{nm} = 2.25 A_{nv} \sqrt{f'_m}$$

$$V_{ns} = 0.5 \left(\frac{A_v}{s} \right) f_y d_v$$

$$V_n \leq 4 A_{nv} \sqrt{f'_m}$$

- d_v = actual depth of masonry
- A_{nv} = net shear area = $b d_v$
 - Many designers use d instead of d_v for beams; clarified in 2022 TMS 402
- $\phi = 0.8$

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Stirrups

Strength Design Guide 6.3.1; TMS 402 Section 9.3.4.2.3

- a) Single bar with 180-degree hook at each end
- b) Hook shear reinforcement around flexural reinforcement
- c) Minimum area of shear reinforcement is $0.0007bd_v$
 - Interpreted as $A_v/s \geq 0.0007b$
- d) First bar within $d_v/4$
- e) Maximum spacing is $d_v/2$ or 48 in.

$$d_{min} = \frac{V_u}{1.8b\sqrt{f'_m}} \quad \text{for no shear reinforcement}$$

Shear at $d/2$

Strength Design Guide 6.4.3.4; TMS 402 Section 8.3.5.4

Sections within $d/2$ from face of support can be designed for shear at $d/2$ (TMS 402 8.3.5.4): (moved to Chapter 5 in 2022 TMS 402)

- A. Noncantilever beam
- B. Reaction introduces compression into end region of member
- C. No concentrated load between $d/2$ and face of support

Design Example

Beam Design

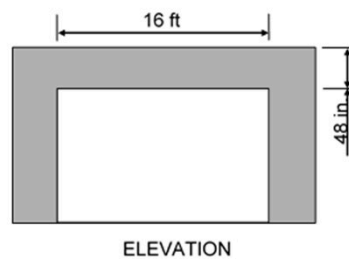
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Design Example

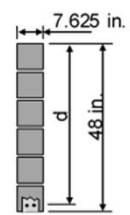
Strength Design Guide Example 6.3.1.8

Given:

- superimposed dead load = 500 lb/ft
- live load = 450 lb/ft
- Grade 60 steel
- Type S PCL mortar
- 8 in. CMU
- $f'_m = 2000$ psi



ELEVATION



CROSS-SECTION

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Design Example: Load

Strength Design Guide Example 6.3.1.8

Span length: Assume not built integrally with support

$$\text{Span length} = 16 \text{ ft} + 2(4 \text{ in.}) = 16.67 \text{ ft}$$

Beam Weight: Assume fully grouted, medium weight units; 81 psf

$$\text{Weight} = 81 \text{ psf}(4 \text{ ft}) = 324 \text{ lb/ft}$$

Factored load, w_u

$$w_u = 1.2D + 1.6L = 1.2 \left(500 \frac{\text{lb}}{\text{ft}} + 324 \frac{\text{lb}}{\text{ft}} \right) + 1.6 \left(450 \frac{\text{lb}}{\text{ft}} \right) = 1,709 \frac{\text{lb}}{\text{ft}}$$

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Design Example: Beam Depth

Strength Design Guide Example 6.3.1.8

Factored shear, V_u

$$V_u = \frac{1,709 \frac{\text{lb}}{\text{ft}} (16.67 \text{ ft})}{2} = 14,240 \text{ lb}$$

Minimum depth to avoid shear reinforcement

$$d_{min} = \frac{V_u}{1.8b\sqrt{f'_m}} = \frac{14,240 \text{ lb}}{1.8(7.625 \text{ in.})\sqrt{2,000 \text{ psi}}} = 23.2 \text{ in.}$$

- 32 in. deep beam is needed
- Prescriptive seismic reinforcement would be needed in top course
- Rather than leave one course ungrouted, fully grout entire height of beam
- Shear strength OK by inspection

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Design Example: Sharpen Pencil

Strength Design Guide Example 6.3.1.8

Try 24 in. deep beam, $d = 20$ in. Check V_u at $d/2$ from face of support

$$\begin{array}{l} d/2 \text{ from face} \\ \text{of support} \end{array} \quad (4in. + 20in.) \frac{1ft}{12in.} = 2.0ft$$

$$\begin{array}{l} \text{Factored} \\ \text{shear, } V_u \end{array} \quad V_u = 14,240lb \frac{8.33ft \cdot .0ft}{8.33ft} = 14,240lb(0.76) = 10,820lb$$

$$d_{min} = \frac{V_u}{1.8b\sqrt{f'_m}} = \frac{10,820lb}{1.8(7.625in.)\sqrt{2,000psi}} = 17.6in.$$

- A 24 in. deep beam will work
- In this example, most engineers would still fully grout the beam, rather than have two ungrouted courses.

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Design Example: Flexure

Strength Design Guide Example 6.3.1.8

$$\begin{array}{l} \text{Factored} \\ \text{moment, } M_u \end{array} \quad M_u = \frac{1,709 \frac{lb}{ft} (16.67ft)^2}{8} \frac{12in.}{ft} = 712,000in. \cdot lb$$

$$\begin{array}{l} \text{Depth of} \\ \text{stress block, } a \end{array} \quad a = d - \sqrt{d^2 - \frac{2M_u}{0.8\phi f'_m b}}$$

$$= 44in. - \sqrt{44in.^2 - \frac{2(712,000in. \cdot lb)}{0.8(0.9)(2,000psi)(7.625in.)}} = 1.50in.$$

$$\begin{array}{l} \text{Required} \\ \text{steel, } A_{s,reqd} \end{array} \quad A_{s,reqd} = \frac{0.8f'_m b a}{f_y} = \frac{0.8(2,000psi)(7.625in.)(1.50in.)}{60,000psi} = 0.305in.^2$$

Try 1 – No. 5

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Design Example: Minimum Reinf.

Strength Design Guide Example 6.3.1.8

Modulus of rupture, Type S PCL mortar: 267 psi

$$\text{Cracking moment, } M_{cr} \quad M_{cr} = f_r S_n = f_r \frac{bh^2}{6} = 267 \text{psi} \frac{7.625 \text{in.} (48 \text{in.})^2}{6} = 782,000 \text{in.} \cdot \text{lb}$$

$$\text{Nominal moment, } M_n \quad M_n = A_s f_y \left(d - \frac{1}{2} \frac{A_s f_y}{0.8 f'_m b} \right) = (0.31 \text{in.}^2) (60,000 \text{psi}) \left(44 \text{in.} - \frac{1}{2} \frac{(0.31 \text{in.}^2) 60,000 \text{psi}}{0.8 (2,000 \text{psi}) (7.625 \text{in.})} \right) = 804,000 \text{in.} \cdot \text{lb}$$

$$M_n = 804 \text{in.} \cdot \text{kip} < 1.3 M_{cr} = 1.3 (782) \text{in.} \cdot \text{kip} = 1,016 \text{in.} \cdot \text{kip} \quad \text{No good}$$

$$\text{Try 2 - No. 4; } M_n = 1,032 \text{in.} \cdot \text{kip} \quad \text{OK}$$

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Design Example: Maximum Reinf.

Strength Design Guide Example 6.3.1.8

$$\text{Reinf. Ratio, } \rho \quad \rho = \frac{A_s}{bd} = \frac{2(0.20 \text{in.}^2)}{7.625 \text{in.} (44 \text{in.})} = 0.00119$$

$$0.00119 \ll 0.00952 \quad \text{OK}$$

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Design Example: Bracing

Strength Design Guide Example 6.3.1.8

$$32b = 32(7.625in.) = 20.3ft$$

$$120b^2/d = 120(7.625in.)^2/44in. = 13.2ft$$

- If top of beam were the roof, that would provide continuous lateral support
- If top of beam were a parapet, provide bracing at midspan and ends

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Design Example: Deflections

Strength Design Guide Example 6.3.1.8

- Beam is not supporting unreinforced masonry, so deflections do not need to be checked
- As a quick check: $l/d = 16.67ft \left(12 \frac{in.}{ft}\right) / 44in. = 4.5 \leq 8$ OK
- Deflection check will be illustrated in next example

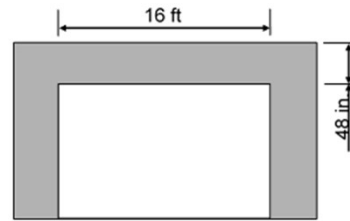
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Design Example

Strength Design Guide Example 6.3.1.9

Given: Modify load

- superimposed dead load = 2,000 lb/ft
- live load = 700 lb/ft



ELEVATION

Factored load, w_u

$$w_u = 1.2D + 1.6L = 1.2 \left(2,000 \frac{lb}{ft} + 324 \frac{lb}{ft} \right) + 1.6 \left(700 \frac{lb}{ft} \right) = 3,910 \frac{lb}{ft}$$

Flexural reinforcement is 4 – No. 4

2 bars in each of bottom two courses

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Design Example: Shear

Strength Design Guide Example 6.3.1.9

Factored shear, V_u

$$V_u = \frac{3,910 \frac{lb}{ft} (16.67 ft)}{2} = 32,600 lb$$

Shear area, A_{nv}

$$A_{nv} = 7.625 in. (40 in.) = 305 in.^2$$

Check max V_n

$$\phi(V_n)_{max} = 4A_{nv}\sqrt{f'_m} = 0.8(4)(305 in.^2)\sqrt{2,000 psi} = 43,600 lb$$

OK

Nominal strength masonry, V_{nm}

$$V_{nm} = 2.25A_{nv}\sqrt{f'_m} = 2.25(305 in.^2)\sqrt{2,000 psi} = 30,700 lb$$

Req'd strength reinf., V_{ns}

$$V_{ns, reqd} = \frac{V_u}{\phi} - V_{nm} = \frac{32,600 lb}{0.8} - 30,700 = 10,100 lb$$

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Design Example: Shear

Strength Design Guide Example 6.3.1.9

Try No. 3 bars for stirrups (deformed wire could also be used).

$$\text{Spacing, } s \quad V_{ns} = 0.5 \left(\frac{A_v}{s} \right) f_y d_v \Rightarrow s = \frac{0.5 A_v f_y d_v}{V_{ns}} = \frac{0.5 (0.11 \text{ in.}^2) (60,000 \text{ psi}) (48 \text{ in.})}{10,100 \text{ lb}} = 15.7 \text{ in.}$$

Try No. 3 at 8 in.

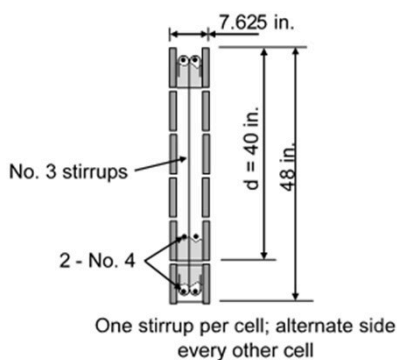
Detailing requirements

- $A_v/s = 0.11 \text{ in.}^2 / 8 \text{ in.} = 0.0138 \text{ in.} \geq 0.0007b = 0.0007(7.625 \text{ in.}) = 0.0053 \text{ in.}$
- First bar located not more than $d_v/4 = 48 \text{ in.} / 4 = 12 \text{ in.}$
- Maximum spacing of $\min\{d_v/2, 48 \text{ in.}\} = \min\{48 \text{ in.} / 2, 48 \text{ in.}\} = 24 \text{ in.}$

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Design Example: Shear Details

Strength Design Guide Example 6.3.1.9



Parameter	Width
Face shell; 1.25 in. each	2.50 in.
Block taper; assume to be 0.25 in. each side	0.50 in.
Thickness of grout between reinforcement and masonry; 0.50 in. (TMS 402 6.1.3.5)	1.00 in.
Stirrup diameter: 2 at 0.375 in.	0.75 in.
Longitudinal reinforcement diameter; 2 at 0.50 in.	1.00 in.
Space between bars; 1.00 in. (TMS 402 6.1.3.1)	1.00 in.
TOTAL	6.75 in.

≤ 7.625 in. OK

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Design Example: Deflections

Strength Design Guide Example 6.3.1.9; Illustration

$$\text{Modulus ratio } n = \frac{E_s}{E_m} = \frac{29000\text{ksi}}{900 \frac{\text{ksi}}{m}} = \frac{29000\text{ksi}}{900(2\text{ksi})} = 16.11$$

$$\text{Reinforcement ratio } \rho = \frac{A_s}{bd} = \frac{4(0.20\text{in.}^2)}{7.625\text{in.}(40\text{in.})} = 0.002623 \quad n\rho = 0.04225$$

$$\text{Find } k = \frac{\sqrt{(n\rho)^2 + 2n\rho} - n\rho}{\sqrt{(0.04225)^2 + 2(0.04225)}} = 0.252 \quad kd = 0.252(40\text{in.}) = 10.06\text{in.}$$

$$\text{Net moment of inertia, } I_n = \frac{bd_y^3}{12} = \frac{7.625\text{in.}(48\text{in.})^3}{12} = 70,270\text{in.}^4$$

$$\text{Cracked moment of inertia, } I_{cr} = \frac{bk^3d^3}{3} + nA_s(d - kd)^2 = \frac{7.625\text{in.}(10.06\text{in.})^3}{3} + 16.11(0.80\text{in.}^2)(40\text{in.} - 10.06\text{in.})^2 = 14,140\text{in.}^4$$

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Design Example: Deflections

Strength Design Guide Example 6.3.1.8

$$\text{ASD load } w = D + L = \left(2,000 \frac{\text{lb}}{\text{ft}} + 324 \frac{\text{lb}}{\text{ft}}\right) + 700 \frac{\text{lb}}{\text{ft}} = 3,020 \frac{\text{lb}}{\text{ft}}$$

$$\text{ASD Moment, } M_a = \frac{wL^2}{8} = \frac{3,020 \frac{\text{lb}}{\text{ft}}(16.67\text{ft})^2}{8} \frac{12\text{in.}}{\text{ft}} = 1,259,000\text{in.} \cdot \text{lb}$$

$$\text{Cracking Moment, } M_{cr} = 782,000\text{in.} \cdot \text{lb} \quad (\text{from minimum reinforcement calc})$$

$$\text{Effective Moment of Inertia, } I_{eff} = I_n \left(\frac{M_{cr}}{M_a}\right)^3 + I_{cr} \left[1 - \left(\frac{M_{cr}}{M_a}\right)^3\right] = 70,270\text{in.}^4 \left(\frac{782\text{in.} \cdot \text{k}}{1,259\text{in.} \cdot \text{k}}\right)^3 + 14,140\text{in.}^4 \left[1 - \left(\frac{782\text{in.} \cdot \text{k}}{1,259\text{in.} \cdot \text{k}}\right)^3\right] = 27,590\text{in.}^4$$

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Design Example: Deflections

Strength Design Guide Example 6.3.1.8

$$\text{Deflection, } \delta = \frac{5wL^4}{384EI} = \frac{5\left(3,020\frac{\text{lb}}{\text{ft}}\right)(16.67\text{ft})^4}{384(1,800,000\text{psi})(27,590\text{in.}^4)} \frac{1728\text{in.}^3}{1\text{ft}^3} = 0.106\text{in.}$$

$$\text{Allowable } \delta = \frac{L}{600} = \frac{16.67\text{ft}}{600} \frac{12\text{in.}}{\text{ft}} = 0.333\text{in.} \quad \text{OK}$$

Quick check using cracked moment of inertia, $\delta = 0.206$ in.

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Deep Beams

- Internal Lever Arm
- Miscellaneous Requirements
- Example

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Internal Lever Arm

Strength Design Guide 6.3.3.6; TMS 402 Section 5.2.2.1, 5.2.2.2

Definition (TMS 402 2.2)

$$\frac{l_{eff}}{d_v} \leq \begin{cases} 3 & \text{continuous span} \\ 2 & \text{simple span} \end{cases}$$

Effective span length, l_{eff} , smaller of:

- center-to-center distance between supports
- 1.15 multiplied by the clear span

z – internal lever arm	
Simple spans	Continuous spans
$1 \leq \frac{l_{eff}}{d_v} < 2 \quad z = 0.2(l_{eff} + 2d_v)$	$1 \leq \frac{l_{eff}}{d_v} < 3 \quad z = 0.2(l_{eff} + 1.5d_v)$
$\frac{l_{eff}}{d_v} < 1 \quad z = 0.6l_{eff}$	$\frac{l_{eff}}{d_v} < 1 \quad z = 0.5l_{eff}$

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Miscellaneous Requirements

Strength Design Guide 6.3.3.6; TMS 402 Section 5.2.2.3, 5.2.2.4, 5.2.2.5

- Flexural reinforcement
 - distributed flexural reinforcement for half beam depth
 - maximum spacing of one-fifth d_v or 16 in.
 - joint reinforcement can be used as flexural reinforcement
 - horizontal reinforcement anchored to develop yield strength at face of supports
- Shear reinforcement (when required)
 - minimum area of vertical reinforcement is $0.0007bd_v$
 - horizontal shear reinforcement area \geq half vertical shear reinforcement
 - maximum spacing of shear reinforcement one-fifth d_v or 16 in.
- Total reinforcement: sum of horizontal and vertical reinforcement at least $0.001bd_v$.

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Design Example

Strength Design Guide Example 6.3.1.7

Given:

- 10 ft opening
- 6 ft deep beam
- superimposed dead load = 3.0 kip/ft
- live load = 2.0 kip/ft
- Grade 60 steel
- Type S masonry cement mortar
- 8 in. CMU
- $f'_m = 2000$ psi

$$\text{C/C between supports} = 10 \text{ ft} + 2(4 \text{ in.}) = 10.67 \text{ ft}$$

$$1.15(\text{clear span}) = 1.15(10 \text{ ft}) = 11.5 \text{ ft}$$

$$\text{Effective span length, } l_{eff} = \min(10.67, 11.5) = 10.67 \text{ ft}$$

$$\text{Span ratio, } \frac{l_{eff}}{d_v} = \frac{10.67 \text{ ft}}{6 \text{ ft}} = 1.78 \leq 2$$

Therefore a deep beam

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Design Example: Flexure

Strength Design Guide Example 6.3.1.7

Beam Weight: Assume fully grouted, medium weight units; 81 psf

$$\text{Weight} = 81 \text{ psf}(6 \text{ ft}) = 0.486 \text{ k/ft}$$

$$\text{Factored load, } w_u = 1.2D + 1.6L = 1.2 \left(3.0 \frac{\text{k}}{\text{ft}} + 0.486 \frac{\text{k}}{\text{ft}} \right) + 1.6 \left(2.0 \frac{\text{k}}{\text{ft}} \right) = 7.38 \frac{\text{k}}{\text{ft}}$$

$$\text{Factored moment, } M_u = \frac{7.38 \frac{\text{k}}{\text{ft}} (10.67 \text{ ft})^2}{8} = 105.0 \text{ k} \cdot \text{ft}$$

$$\text{Internal lever arm, } z = 0.2(l_{eff} + 2d_v) = 0.2(10.67 \text{ ft} + 2(6 \text{ ft})) = 4.53 \text{ ft}$$

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Design Example: Flexure

Strength Design Guide Example 6.3.1.7

$$\text{Req'd } A_s \quad A_{s,reqd} = \frac{M_u/\phi}{zf_y} = \frac{105.0k \cdot ft/0.9}{4.53ft(60ksi)} = 0.429in.^2$$

Using standard beam theory would have $A_{s,reqd}$ underestimated by 14%.

Although 1-#6 could be used, use 2-#5, one in each of bottom two courses

- reduces development length and extension of bars beyond face of support
- helps with requirement of distributed reinforcement

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Design Example: Reinforcement

Strength Design Guide Example 6.3.1.7

$$\rho_{max} \quad d = 72in. - 8in. = 64in. \quad \text{distance to centroid of reinforcement}$$

$$\rho = \frac{A_s}{bd} = \frac{2(0.31in.^2)}{7.625in.(64in.)} = 0.00127 \leq 0.00952$$

$$\rho_{min} \quad A_s = 0.62in.^2 \geq \frac{4}{3}A_{s,reqd} = \frac{4}{3}(0.43in.^2) = 0.57in.^2$$

Distributed reinforcement: required over bottom half of beam at a spacing of $1/5d_v = 1/5(72in.) = 14.4in.$, but not greater than 16 in.

Use W1.7 (9 gage) joint reinforcement every 8 in. in bottom five bed joints.

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Design Example: Development

Strength Design Guide Example 6.3.1.7

$$\text{Development length, } l_{de} = \frac{0.13d_b^2 f_y \gamma}{K \sqrt{f'_m}} = \frac{0.13(0.625 \text{ in.})^2 (60,000 \text{ psi})(1.0)}{\min\{9(0.625 \text{ in.}), 3.81 \text{ in.} - 0.625 \text{ in.}/2\} \sqrt{2,000 \text{ psi}}} = 19.5 \text{ in.}$$

- Extend bars 20 in. beyond face of support
- Details of development length will be covered in Session 6

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Design Example: Shear

Strength Design Guide Example 6.3.1.7

$$\text{Factored shear, } V_u = \frac{7.38 \frac{k}{ft} (10.67 ft)}{2} = 39.4 \text{ kip}$$

$$\begin{aligned} \text{Design shear strength from masonry, } \phi V_{nm} &= \phi 2.25 A_{nv} \sqrt{f'_m} \\ &= 0.8(2.25)(7.625 \text{ in.})(68 \text{ in.}) \sqrt{2000 \text{ psi}} = 41.7 \text{ k} \end{aligned}$$

Since $\phi V_{nm} \geq V_u$ no shear reinforcement required

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Design Example: Total Reinforcement

Strength Design Guide Example 6.3.1.7

Total
Reinforcement $0.001bd_v = 0.001(7.625in.)(72 in.) = 0.55in.^2$

2 - #5 meets total reinforcement by inspection.

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This concludes The American Institute of Architects Continuing Education
Systems Course



The Masonry Society

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